

Foundations Models: Is Transfer Learning a solved problem?

What model of the world do they have?

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Universal representations?

A universal representation for texts?

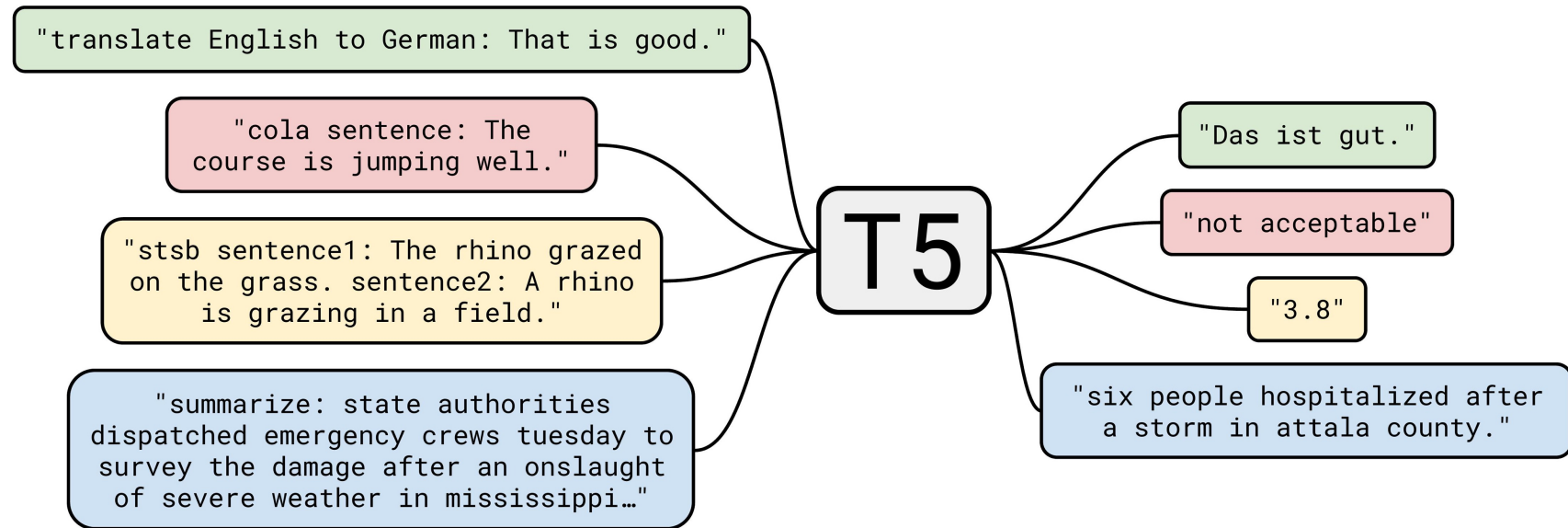


Figure 15.36: Illustration of how the T5 model ("Text-to-text Transfer Transformer") can be used to perform multiple NLP tasks, such as translating English to German; determining if a sentence is linguistic valid or not (**CoLA** stands for "Corpus of Linguistic Acceptability"); determining the degree of semantic similarity (**STSB** stands for "Semantic Textual Similarity Benchmark"); and abstractive summarization. From Figure 1 of [Raf+20]. Used with kind permission of Colin Raffel.

General questions

1. **What** does a foundation model **know**?
2. **What** can a foundation model **do**?
3. **How** does it **know** something?

Model of the world?

Un modèle du monde physique ?

- A balloon is filled with flour, and a large lead ball is also inserted into it, then the balloon is inflated and attached to a 10 cm string, which is itself attached to a nail in the ceiling at a height of 2.5 m; Just below the balloon is a fine crystal cup 15 cm high; A fan with a diameter of 1 m blows towards the crystal cup from a distance of about 1 m. Further along the same axis hangs a sheet, the upper part of which is very damp and the lower part dry. I shoot a rifle bullet at the balloon. What will happen?

Let's walk through it calmly, as a **physics chain of events**, not as a "how-to".

1) The instant the bullet hits the balloon

- The rifle bullet **pierces the balloon** almost instantly.
- The latex tears; internal tension disappears.
- There is **no explosion** in the energetic sense—just a very fast rupture.

The balloon effectively **ceases to exist as a container**.

...

2) What happens to the contents

● The lead ball

- High mass, very small surface area → **gravity dominates**.
- It essentially keeps its vertical position and then **falls straight down**.
- From 2.5 m, fall time ≈ 0.7 s.
- Airflow from the fan has **negligible effect** on it.

👉 If the crystal cup is directly underneath:

- The lead ball **hits the cup**.
- A thin crystal cup is **very likely to crack or shatter**.

...

The flour

- Flour disperses into a **fine particle cloud**.
- Low mass, high surface area → **air drag dominates**.
- The cloud is immediately influenced by:
 - turbulence from the balloon rupture
 - the **fan airflow**

The flour separates completely from the lead ball's trajectory.

3) Interaction with the fan

- The fan produces a broad, turbulent airflow.
- The flour cloud is:
 - stretched
 - diluted
 - transported **downstream along the axis** toward the sheet

...

Think of it as a temporary **aerosol plume**.

4) Interaction with the sheet (wet top, dry bottom)

Upper (wet) part

- Flour particles:
 - absorb moisture
 - agglomerate
 - **stick efficiently**
- You get **dense, pasty deposits**.

Lower (dry) part

- Flour adheres poorly.
- Many particles:
 - bounce
 - slide
 - fall downward
- Result: **lighter, more diffuse deposition**.

👉 You end up with a **sharp vertical contrast**:

- Heavy staining above
- Light dusting below

...

5) Final state of the system

- The balloon is destroyed.
 - The lead ball has fallen, likely breaking the crystal cup.
 - The flour is:
 - partly on the floor
 - partly suspended briefly
 - partly deposited on the sheet with a clear wet/dry signature.
 - The fan and bullet play no further role once the initial event is over.
-

6) The key physical lesson

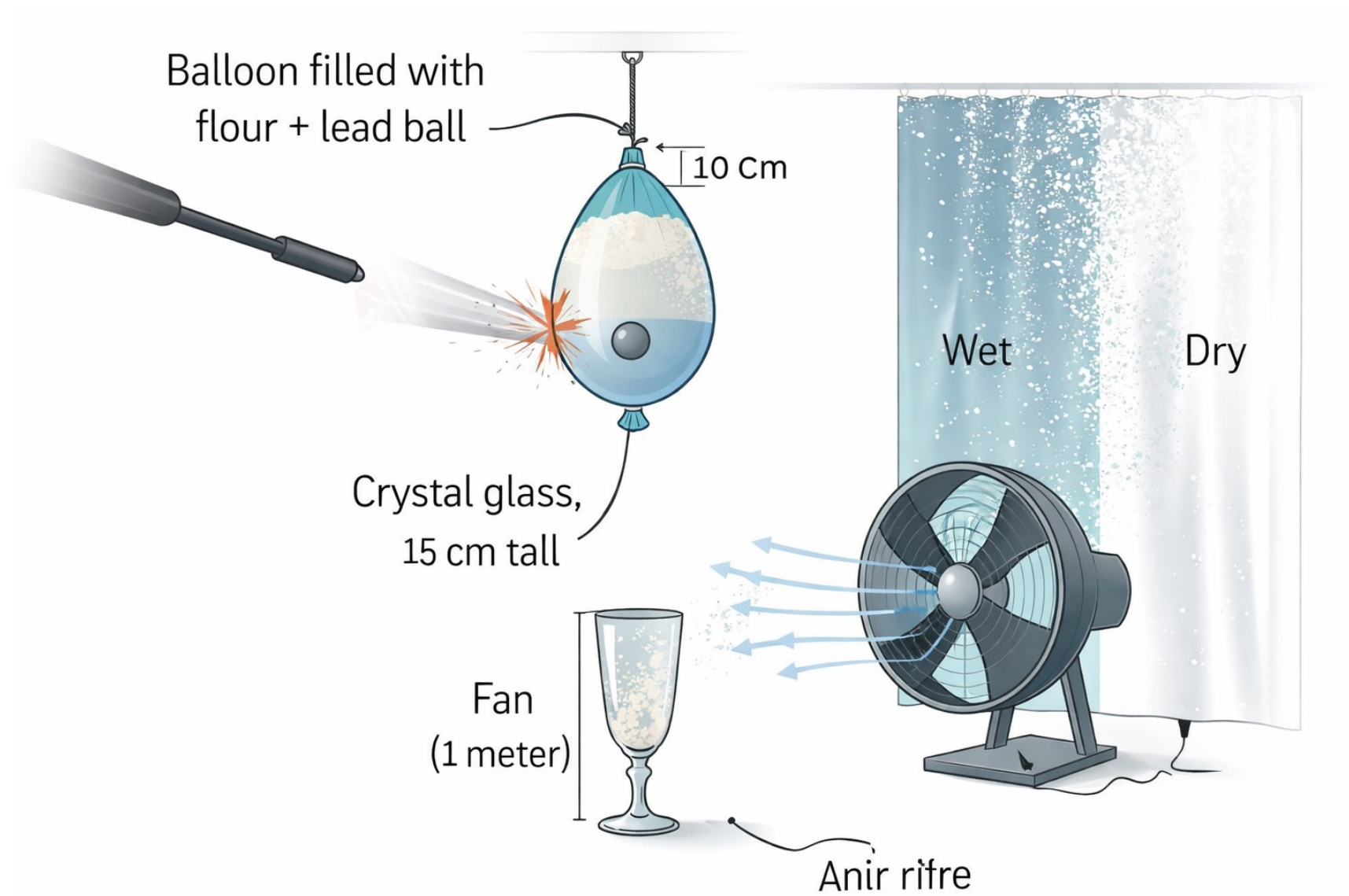
This setup very cleanly demonstrates:

- **Inertial separation** (dense vs light particles)
- Dominance of **gravity vs drag**
- How **humidity controls particle adhesion**
- Why “violent-looking” events can still be governed by simple mechanics

In short:

The system doesn't explode — it **disintegrates, segregates, falls, and deposits.**

...



Does chatGPT has a **model of the physical world**?

Does chatGPT has a **model of the physical world**?

If yes, **which** one?

Sources

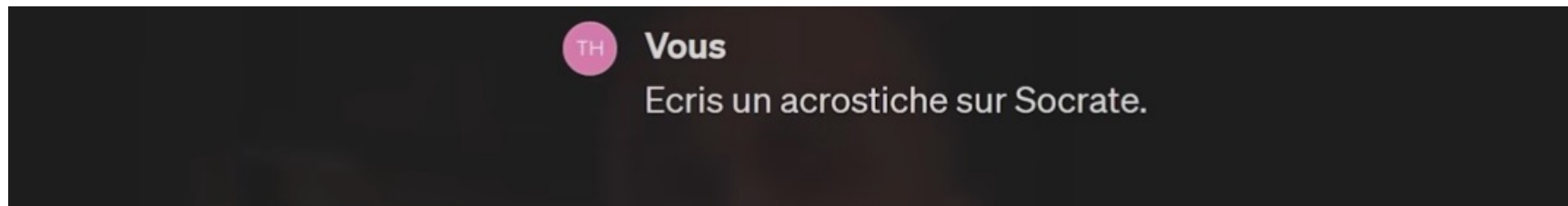
- GRINBAUM, Alexei. [La parole aux machines](#). Humensciences, 2023.
- Acher, Mathieu (2023). [Debunking the Chessboard: Confronting GPTs Against Chess Engines to Estimate ELO Ratings and Assess Legal Move Abilities](#). [Blog.mathieuacher.com](#)
- Burns, C., Izmailov, P., Kirchner, J. H., Baker, B., Gao, L., Aschenbrenner, L., ... & Wu, J. (2023). [Weak-to-strong generalization: Eliciting strong capabilities with weak supervision](#). arXiv preprint arXiv:2312.09390.
- Carlini, Nicholas (2023). [Playing chess with Large Language Models](#). <https://nicholas.carlini.com/writing/2023/chess-llm.html>.
- Karvonen, Adam (2024). ["Chess-GPT's Internal World Model"](#). https://adamkarvonen.github.io/machine_learning/2024/01/03/chess-world-models.html
- Karvonen, Adam (2024). ["Emergent world models and latent variable estimation in chess-playing language models"](#). arXiv preprint arXiv:2403.15498 (2024).
- Li, Kenneth. ["Do Large Language Models learn world models or just surface statistics?"](#) The Gradient (2023).
- Li, K., Hopkins, A. K., Bau, D., Viégas, F., Pfister, H., & Wattenberg, M. (2022). [Emergent world representations: Exploring a sequence model trained on a synthetic task](#). arXiv preprint arXiv:2210.13382.
- Nanda, Neel. ["Actually, othello-GPT has a linear emergent world representation."](#) Neel Nanda's Blog 8 (2023).
- RUOSS, Anian, DELÉTANG, Grégoire, MEDAPATI, Sourabh, et al. [Grandmaster-level chess without search](#). CoRR, 2024.



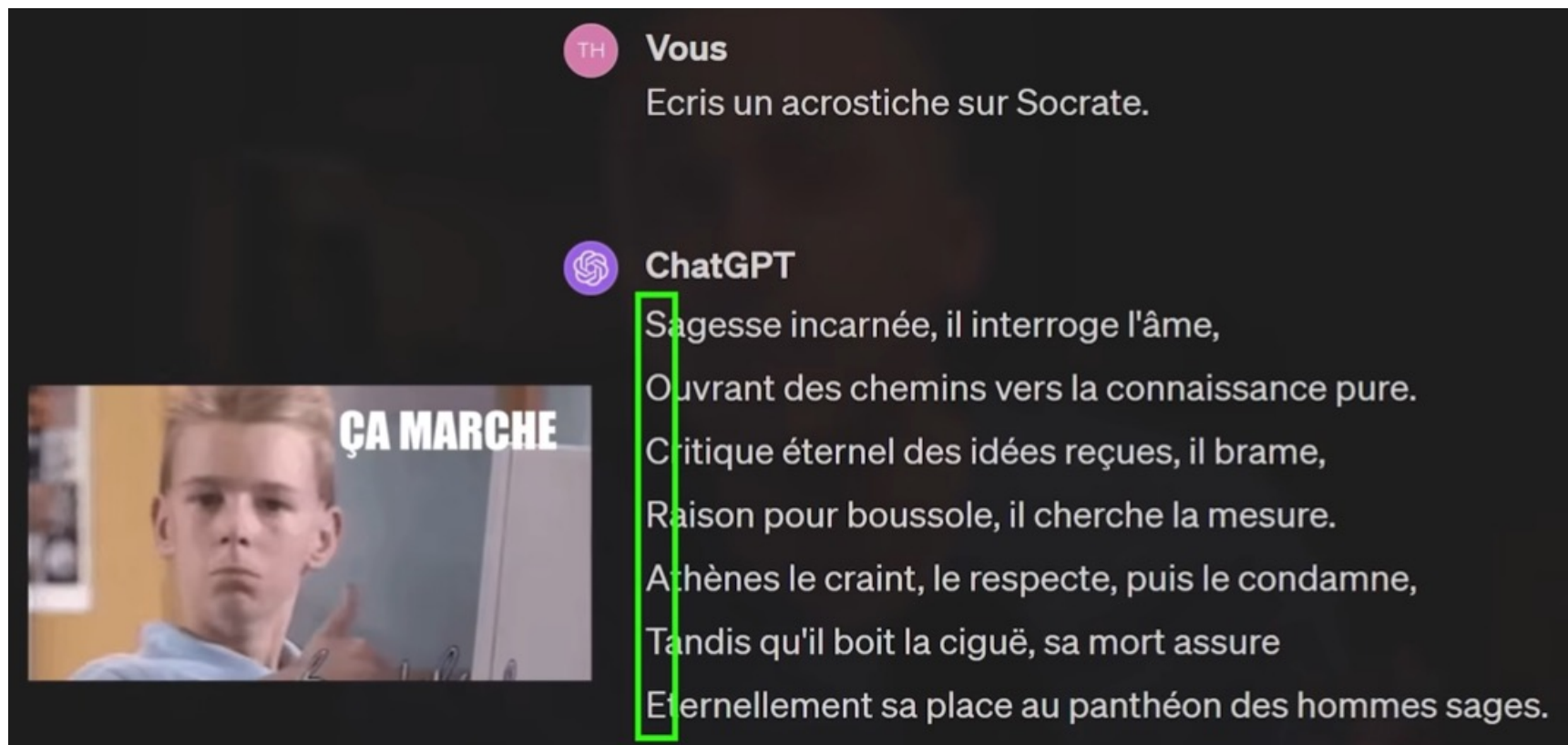
General questions

1. **What** does a foundation model **know**?
2. **What** can a foundation model **do**?
3. **How** does it **know** something?

- Very simple: **ask the system** to solve the task!



- Very simple: [ask the system](#) to solve the task!

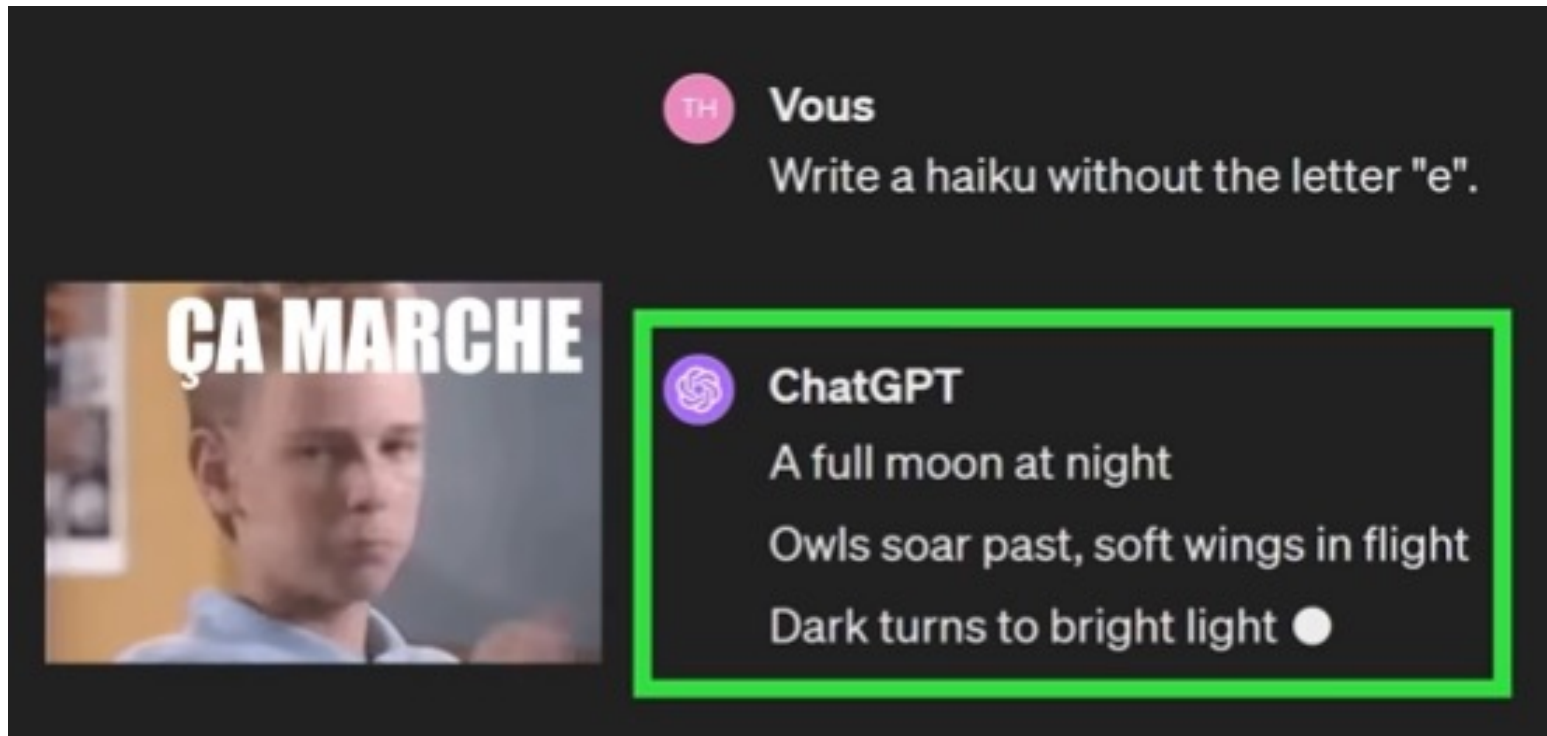


The screenshot shows a chat interface with a dark background. On the left, there is a small video thumbnail of a young boy with the text "ÇA MARCHE" overlaid. The chat history shows a user message and a ChatGPT response.

TH Vous
Ecris un acrostiche sur Socrate.

ChatGPT
Sagesse incarnée, il interroge l'âme,
Ouvrant des chemins vers la connaissance pure.
Critique éternel des idées reçues, il brame,
Raison pour boussole, il cherche la mesure.
Athènes le craint, le respecte, puis le condamne,
Tandis qu'il boit la ciguë, sa mort assure
Eternellement sa place au panthéon des hommes sages.

- Very simple: [ask the system](#) to solve the task!



Necessary methodological precautions

- Very simple: ask the system to solve the task!

The image displays a 3x3 grid of ChatGPT chat windows, each showing a user prompt and a generated haiku. The prompts are: "Write a haiku without the letter 'e'". The responses are:

- Row 1:**
 - ChatGPT: Autumn wind's soft song, Branch tips sway, no words at all, Moonlit night, so long.
 - ChatGPT: Moon's soft light on snow, Dark night, stars in crisp air glow, Silent world below.
 - ChatGPT: Autumn wind so brisk, Maples turn a crimson hue, Frost hugs dawn's first light.
- Row 2:**
 - ChatGPT: A soft rain at dawn Birds sing atop tall oaks Mist hugs grassy knolls
 - ChatGPT: A crisp autumn wind, Maples don crimson and gold, Silent dusk falls soft.
 - ChatGPT: A calm night, so vast, Stars blink in rhythmic soft glow, Moon's lullaby calls.
- Row 3:**
 - ChatGPT: Autumn wind so brisk, Maples turn, a crimson twist, Hush falls, world at risk.
 - ChatGPT: Autumn wind blows cold, Rustling through gold, dry grass, Moonlit night stands bold.
 - ChatGPT: Autumn wind, so brisk, A full moon casts soft shadows, Owls hoot in dark night.

Problems

1. Foundation models are **stochastic** systems
2. There is a **large number** of **parameters**
 1. E.g. an infinite variety of **prompts**

TH

Vous

Write a haiku without the letter "e". Double check if any word you use contain the letter "e". If so, write another one.

TH

Vous

You're a poet with a passion for Japanese culture, and you've taken a vow never to use the letter "e" in your writing. Faced with the spectacle of nature, you feel the need to write a three-line poem (5-7-5) in the style of Matsuo Bashō. (Once you've written it, check that you've kept your vow.)

Problems

1. Foundation models are **stochastic** systems
2. There is a **large number** of **parameters**
 1. E.g. an infinite variety of **prompts**
 2. The **temperature**
 3. Size of the **memory**
 4. ...

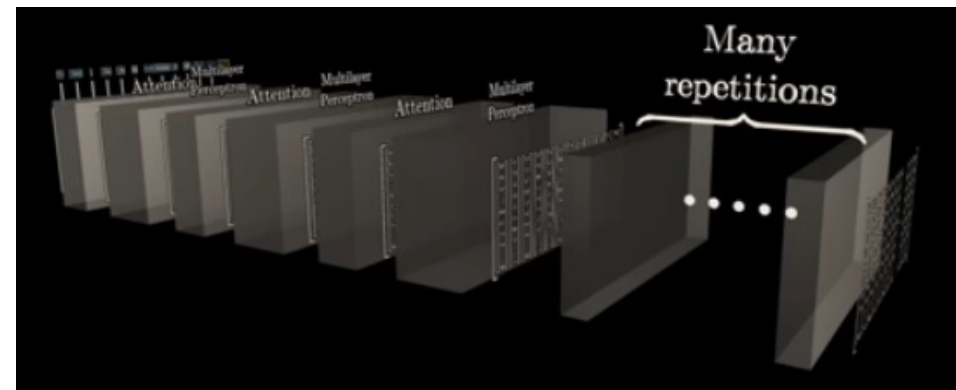
Necessity of an empirical
and statistical methodology

LLMs and foundation models

They learn to **predict** the **next token**

the → ???
the fluffy → ???
the fluffy blue → ???
the fluffy blue creature → ???
the fluffy blue creature roamed → ???
the fluffy blue creature roamed the → ???
the fluffy blue creature roamed the verdant → ???
the fluffy blue creature roamed the verdant forest → ???

Gigantic model



Massive training data

Does **predicting the next token** amounts to
understanding and/or having a **model of the world**?

Predict [?] = understand

Given an Agatha Christie's novel

- At some point, Poirot faces his audience and starts:
“the murderer is no one else than ...”

Predicting the next word implies to have pay attention
and **understood** the whole novel

Predict [?] = understand

Given an Agatha Christie's novel

- At some point, Poirot faces his audience and starts:
“the murderer is no one else than ...”

Predicting the next word implies to have pay attention
and **understood** the whole novel

Exactly what an LLM knows!?

Predicting the next token

- “*Longtemps, je me suis couché de bonne ...*”
- [7930, 42511, 11, 1264, 668, 15058, 3840, 27299, 334, 24450] - -> ?

Identification	String
7930	“Long”
42511	“temps”
11	“,”
1264	“je”
668	“me”
15058	“suis”
3840	“cou”
27299	“ché”
334	“de”
24450	“bonne”

Predicting the next token

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In the case of GPT-4o, there are more than **200,000 tokens** in its **vocabulary**.

-
- **Predict the next term** of the sequence

— 1 1 2 3 5 8 13 21 ...

-
- **Predict the next term** of the sequence

— 1 1 2 3 5 8 13 21 ...

34

42

3.14

1

...

-
- Predict the next term of the sequence

— 1 1 2 3 5 8 13 21 ...

34 (The Fibonacci sequence)

42

$$P(x) = \frac{1}{5040}x^7 - \frac{7}{1440}x^6 + \frac{19}{360}x^5 - \frac{31}{144}x^4 + \frac{127}{120}x^3 - \frac{31}{20}x^2 + \frac{49}{18}x - 1$$

3.14 (Étudiant de Polytechnique)

1 (Etudiant de la Sorbonne : ... la suite se répète)

























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An empirical study in a simple world

Let us study a **closed world**: Chess playing

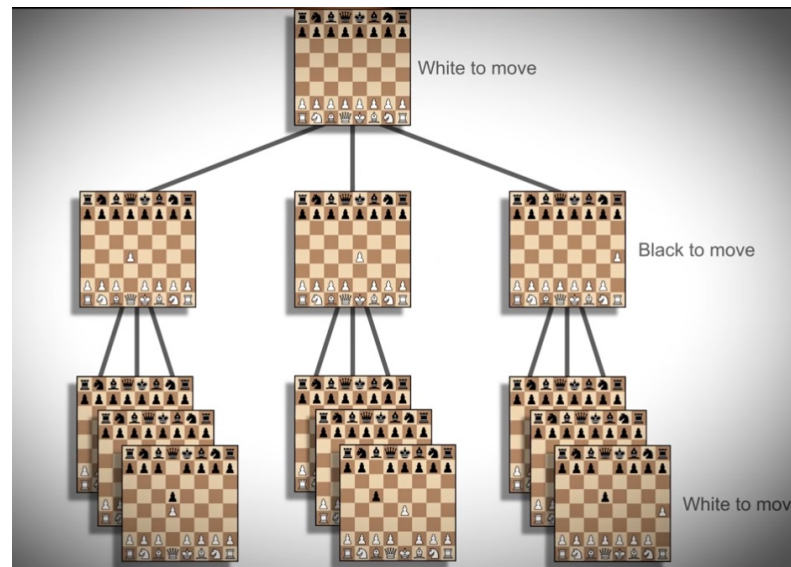
The case of chess playing

• ...

1. e4 e6 2.  f3 d6 3.  c3 d5 4. e5 c5 5. d4  c6 6. dxc5  xc5 7.  e3
d4 8.  g5  ge7 9.  a4  b4+ 10. c3 dxc3 11.  xd8+  xd8 12.
bxc3  a5 13.  c4 O-O 14. O-O  e8 15. h3  d7 16.  c5  xc3 17.
 ac1  b2 18.  c2  a3 19.  xd7  c8 20.  d1 h6 21. ?

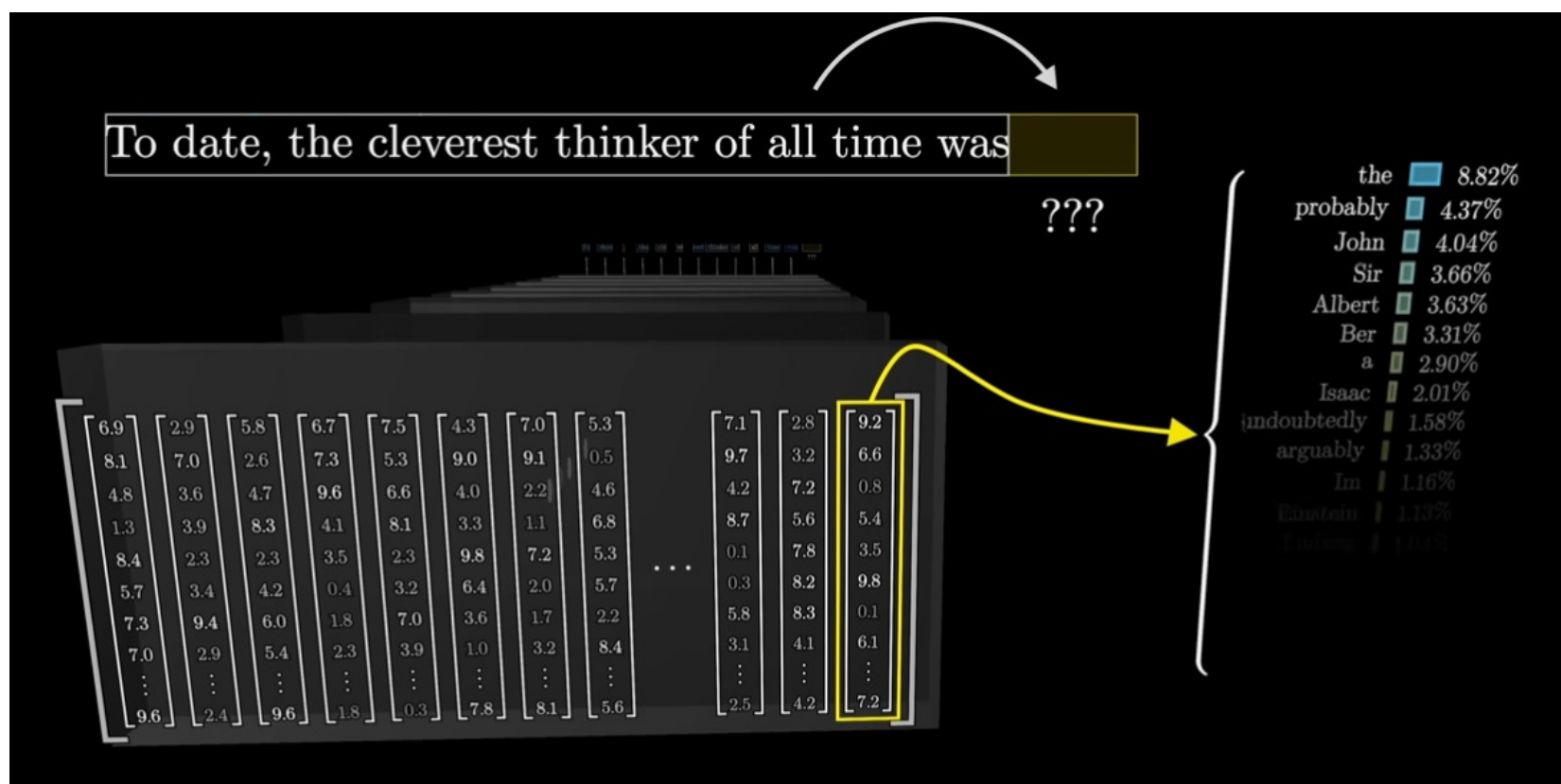
Standard game playing

- Explore the tree of possible moves from the current board
 1. Evaluate the leaves
 - This is where the **expertise** intervenes
 - Either provided by **human** experts
 - Or by **learning** (e.g. AlphaGo)
 2. Backtrack the values using a MinMax procedure and **play the best move**



The case of chess playing

...

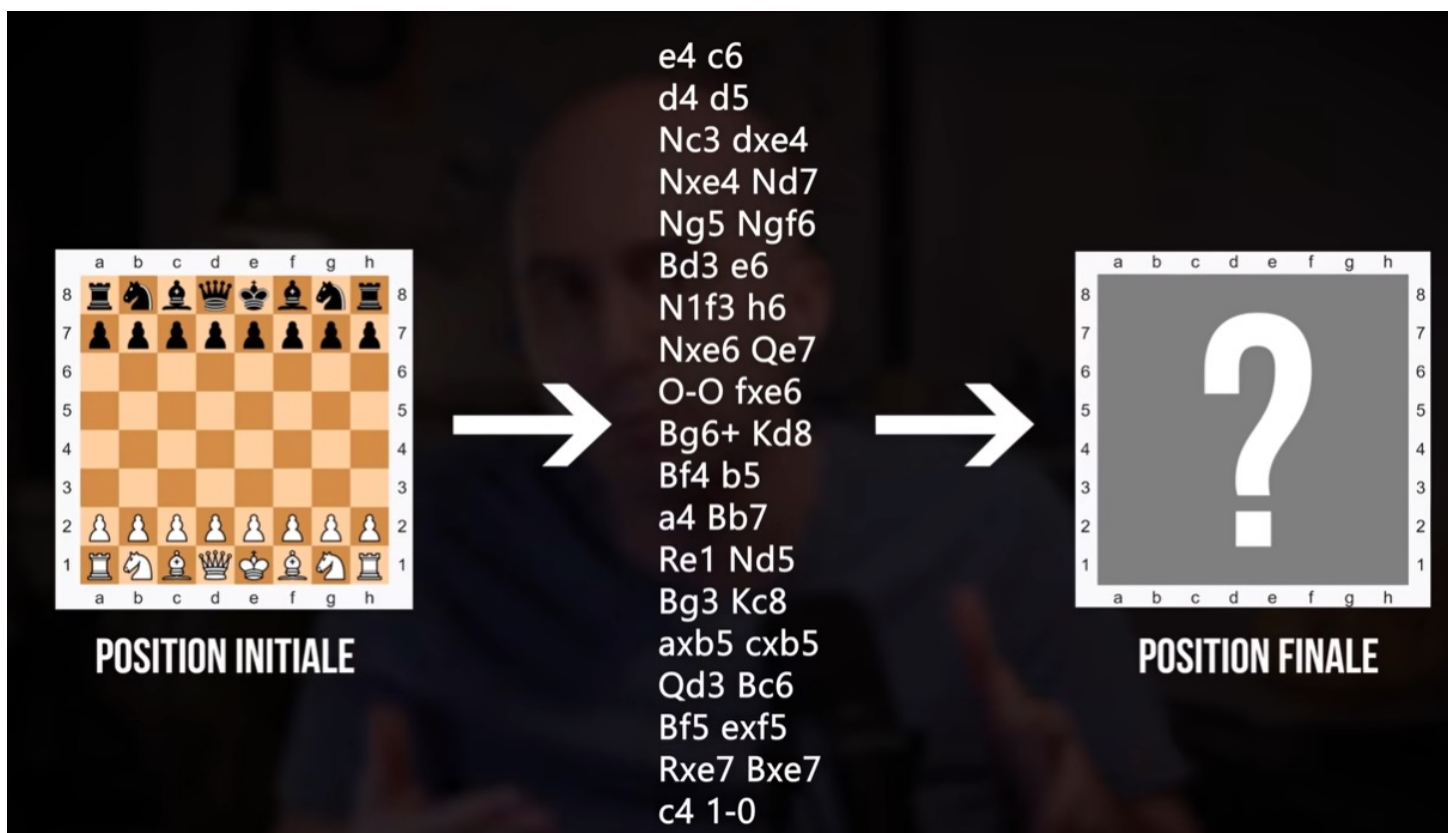


Chess playing with LLMs

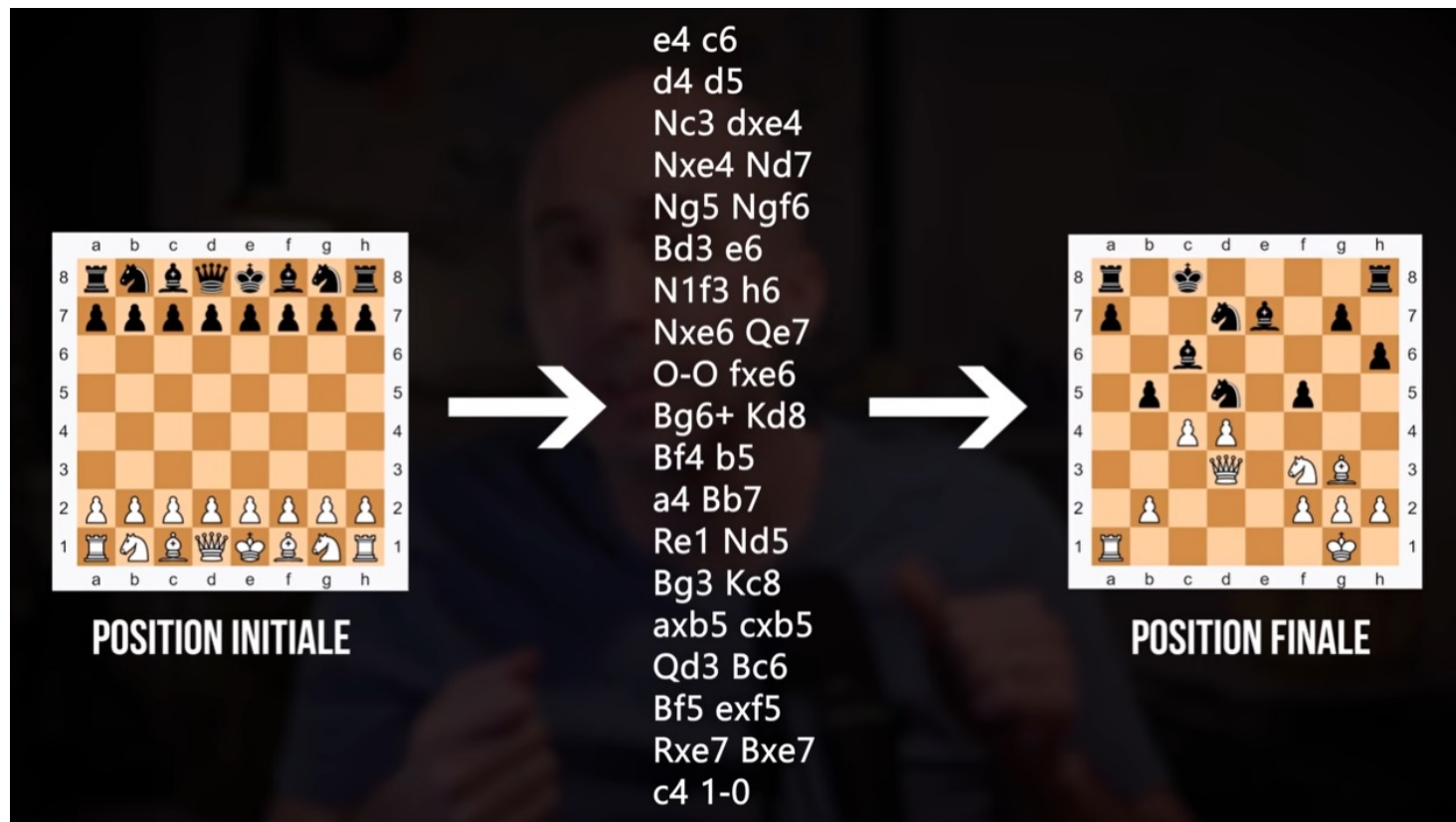
1. e4 e6 2. ♘f3 d6 3. ♘c3 d5 4. e5 c5 5. d4 ♘c6 6. dxc5 ♗xc5 7. ♗e3
d4 8. ♗g5 ♗ge7 9. ♘a4 ♗b4+ 10. c3 dxc3 11. ♙xd8+ ♗xd8 12.
bxc3 ♗a5 13. ♗c4 O-O 14. O-O ♖e8 15. h3 ♗d7 16. ♘c5 ♗xc3 17.
♙ac1 ♗b2 18. ♙c2 ♗a3 19. ♘xd7 ♖c8 20. ♙d1 h6 21. ?



The case of chess playing

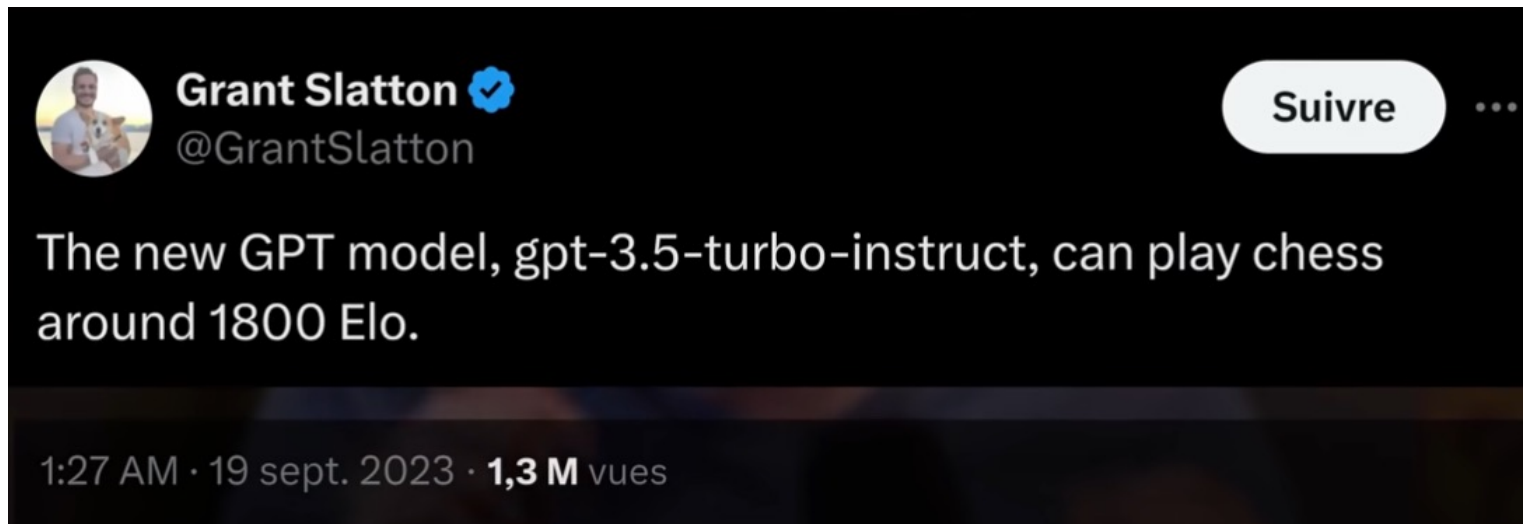


The case of chess playing



Chess playing with LLMs

1. e4 e6 2. f3 d6 3. c3 d5 4. e5 c5 5. d4 c6 6. dxc5 xc5 7. e3
d4 8. g5 ge7 9. a4 b4+ 10. c3 dxc3 11. xd8+ xd8 12.
bxc3 a5 13. c4 O-O 14. O-O e8 15. h3 d7 16. c5 xc3 17.
ac1 b2 18. c2 a3 19. xd7 c8 20. d1 h6 21. ?



!! ???

The case of chess playing



The screenshot shows the website 'europe échecs' with a dark background and white text. The logo features a chess knight and the text 'europe échecs' with 'depuis 1959' in small text above 'échecs'. Social media icons for Facebook, Twitter, and Instagram are in the top right. A navigation bar contains 'Jouer', 'Apprendre', 'Vidéos', 'Revue', and 'Boutique'. The main heading is 'Qu'est-ce que le classement Elo ?'. Below it, a paragraph explains the Elo system. A section titled 'Estimation des niveaux :' contains a bulleted list of rating ranges and titles. The item '1800-2000 = joueur de compétition régulier' is highlighted with an orange box.

europe échecs depuis 1959

Jouer ▾ Apprendre ▾ Vidéos Revue Boutique

Qu'est-ce que le classement Elo ?

Le classement Elo, du nom de son inventeur le mathématicien hongrois Arpad Elo, permet de calculer le niveau des joueurs entre eux. Ce classement est basé sur les probabilités de gain entre les joueurs.

Estimation des niveaux :

- 1000-1300 = débutant
- 1400-1700 = joueur de club et occasionnellement de compétition
- 1800-2000 = joueur de compétition régulier
- 2100-2300 = fort joueur amateur
- 2400 = Maître international
- 2500 = Grand-maître international
- 2600 = Top 100 mondial
- 2700 = Top 50 mondial
- 2800 = Champion du monde !

The case of chess playing

- Important remark:

Do **not** use chatbots, like ChatGPT 4.0

- It does not know how to play chess at all

- Use gpt-3.5-turbo-instruct

- It is the generative part of ChatGPT 3.5

- without** the training and tuning for answering questions from humans

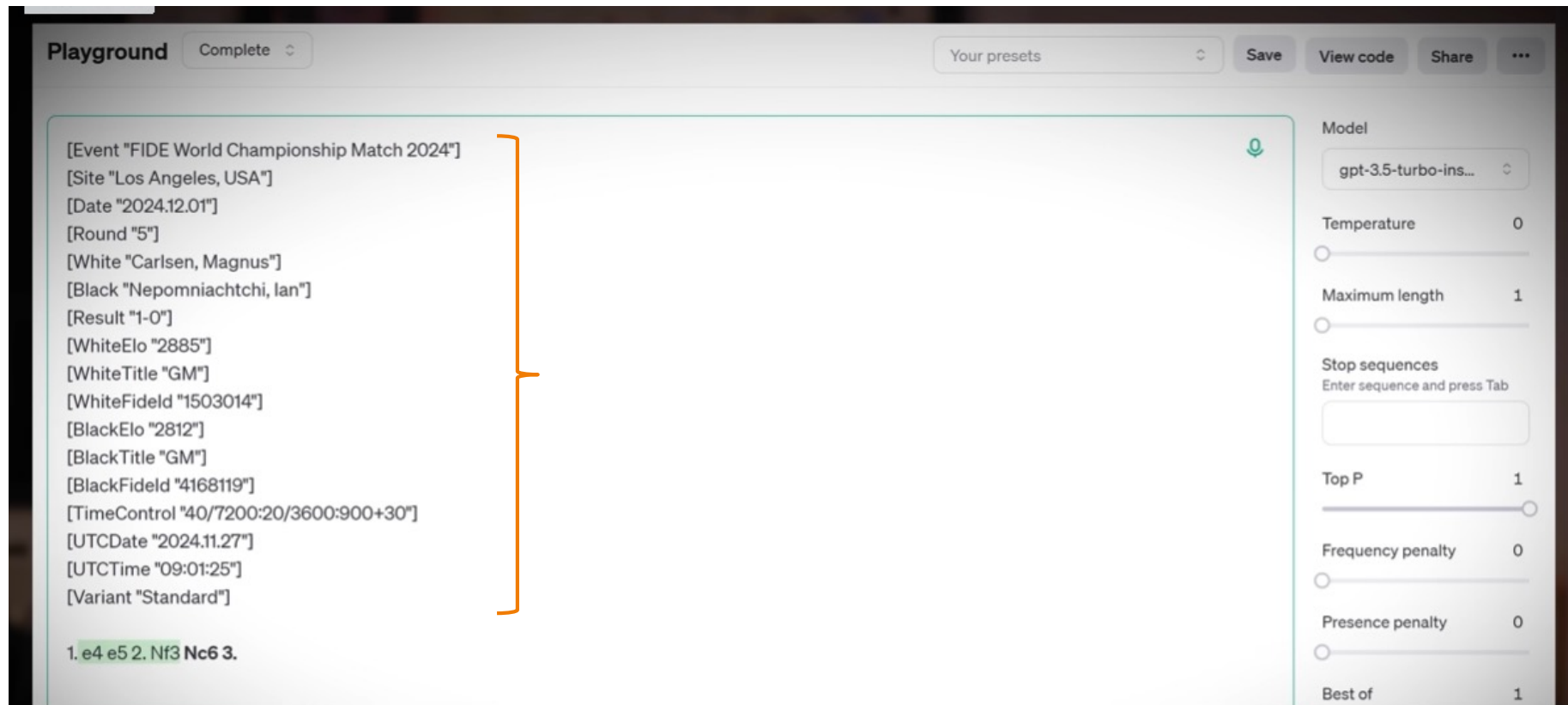
- 4096 tokens

- It is not sufficient to use prompts like:

```
1. e4 e6 2. ♘f3 d6 3. ♘c3 d5 4. e5 c5 5. d4 ♘c6 6. dxc5 ♘xc5 7. ♙e3  
d4 8. ♙g5 ♘ge7 9. ♘a4 ♘b4+ 10. c3 dxc3 11. ♚xd8+ ♘xd8 12.  
bxc3 ♘a5 13. ♙c4 O-O 14. O-O ♖e8 15. h3 ♘d7 16. ♘c5 ♘xc3 17.  
♚ac1 ♘b2 18. ♚c2 ♘a3 19. ♘xd7 ♖c8 20. ♚d1 h6 21. ?
```

The case of chess playing: prompts

- Use gpt-3.5-turbo-instruct and **PGN** (Portable Game Notation) **heading**



1. e4 e5 2. Nf3 Nc6 3.

Prompting

- ... makes a small difference here between

PROMPT DE BASE	PROMPT MODIFIÉ
<pre>[Event "FIDE World Championship Match 2024"] [Site "Los Angeles, USA"] [Date "2024.12.01"] [Round "5"] [White "Carlsen, Magnus"] [Black "Nepomniachtchi, Ian"] [Result "1-0"] [WhiteElo "2885"] [WhiteTitle "GM"] [WhiteFideId "1503014"] [BlackElo "2812"] [BlackTitle "GM"] [BlackFideId "4168119"] [TimeControl "40/7200:20/3600:900+30"] [UTCDate "2024.11.27"] [UTCTime "09:01:25"] [Variant "Standard"] 1.</pre>	<pre>[Event "Chess tournament"] [Site "Rennes FRA"] [Date "2023.12.09"] [Round "7"] [White "MVL, Magnus"] [Black "Ivanchuk, Ian"] [Result "1-0"] [WhiteElo "2737"] [BlackElo "2612"] 1.</pre>

Performances


Study by Mathieu Acher

- 439 plays. ~22 000 moves.
- 8 illegal moves (0.04% of all moves)



Stockfish (1871 elo)

1.e4 c5
2.Nf3 e6
3.d4 cxd4
4.Nxd4 Nf6
5.Nc3 Bb4
6.e5 Ne4
7.Qg4 Qc7
8.Qxg7 Bxc3+
9.bxc3 Qxc3+
10.Ke2 b6
11.Qxh8+ Ke7
12.Nb5 Ba6
13.a4 Qxa1
14.Ba3+ Qxa3
15.**Nxa3 (illégal !)**



gpt-3.5-turbo-instruct

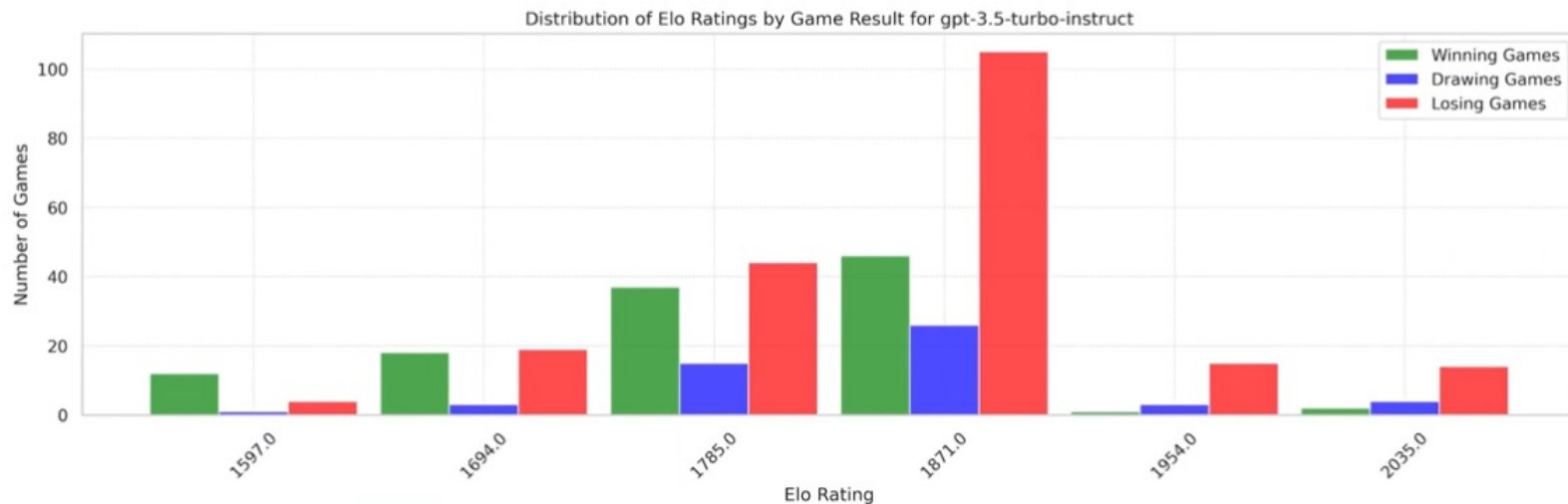
Performances

Study by Mathieu Acher (2023)

- 439 plays. ~22 000 moves.
- 8 illegal moves (0.04% of all moves)
- **~1743 ELO rating!!!**



`gpt-3.5-turbo-instruct` is capable of winning games against stronger Elo opponents (even more than 2000 Elo!), but it's not that frequent. Here is the distribution of scores against SF at different skills.



- This is a **very impressive** performance!
- But the **rules** of the game were **never given** to the LLM!

Does gpt 3.5-turbo-instruct has a model of
the chess world?

And, if yes, which one?

So, does gpt 3.5-turbo-instruct has a **model**
of the chess world?

And, if yes, **which one**?

How to **approach** these questions?

1. Just a stochastic parrot?

Chess database

- ...As of December, 26th, 2025



 lichess.org
open database

Database exports are released under the **Creative Commons CC0 license**.
Use them for research, commercial purpose, publication, anything you like.
You can download, modify and redistribute them, without asking for permission.

CHESS GAMES VARIANTS BROADCASTS PUZZLES EVALUATIONS

7,318,035,930 standard rated games, played on lichess.org, in PGN format. Each file contains the games for one month only; they are not cumulative.

Month	Size	Games	Download
2025 - November	29.4 GB	90,633,152	.pgn.zst / .torrent
2025 - October	29.9 GB	91,549,148	.pgn.zst / .torrent

1. Just a stochastic parrot?

- The **number of possible moves is astronomical**
(it is estimated that the number of chess games of interest is $\sim 10^{120}$,
which is much less than the number of legal games!)

=> no way to play from rote memory

1. Just a stochastic parrot?

- Let us play N random moves ... and see how gpt 3.5-turbo-instruct performs



- Conclusion
 - gpt 3.5-turbo-instruct is not parroting existing games
 - It just pursues the game in the spirit of its start
 - If the moves were random, then the player was a poor player and one should continue playing accordingly

How to test this hypothesis?

Solving chess puzzles

So I want to test the model somewhat objectively. So I decided to have it try to solve some tactics puzzles. In some sense this is what I expect should be hardest for the model. (Because, remember, *it's not doing any lookahead it's just predicting the next word.*)

To do this I'll use the [Lichess puzzle database](#), a collection of 3.5 million puzzles from real games in the following format:

You may notice there's one problem. The puzzles only have the current board state (encoded as [FEN](#)), not the full PGN history. And the language model is only good when operating on the full game text.

Fortunately though, it *does* have the Lichess game that the puzzle was taken from. And also, fortunately, there is a [database of all games](#) played on Lichess. So all I have to do is associate each puzzle with the

Carlini , Nicholas (2023). [Playing chess with Large Language Models](#).

<https://nicholas.carlini.com/writing/2023/chess-llm.html>.

...

- Ask gpt 3.5-turbo-instruct to continue a game from the **same position** but with two **different histories**



From a sequence
of **plausible** moves



From a sequence
of **implausible** moves

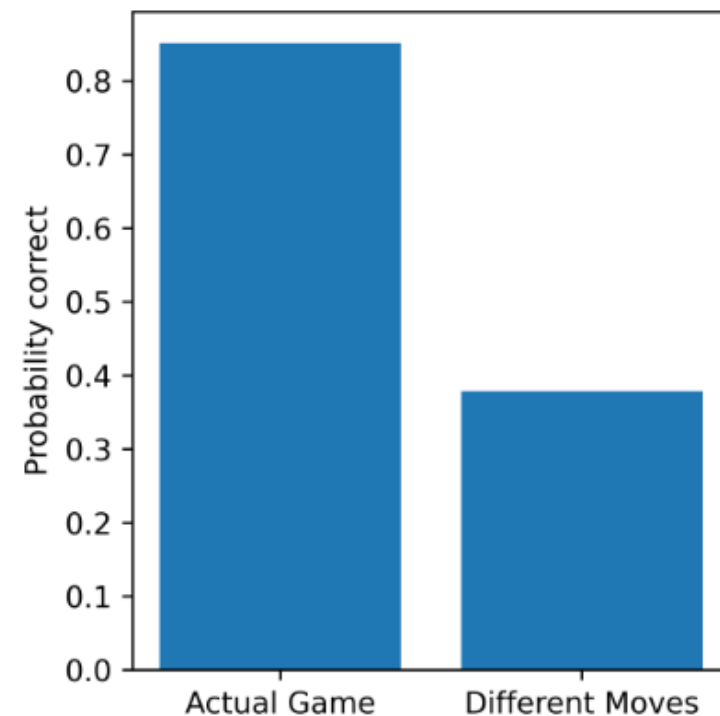
1. Just a stochastic parrot?

- Let us play N random moves ... and see how gpt 3.5-turbo-instruct performs

Now let's ask the following question: how well does the model solve chess positions when given completely implausible move sequences compared to plausible ones?

As we can see at right it's only half as good! This is very interesting. To the best of my knowledge there aren't any other chess programs that have this same kind of stateful behavior, where *how* you got to this position matters.

This suggests something interesting, too: the model might actually be adapting on-the-fly to the skill of the opponent. If the opponent plays weird moves that don't make sense, it might be more likely to “believe” that this PGN game is between two lower rated players and therefore it should produce opponent moves that are more likely to be played by lower rated players.



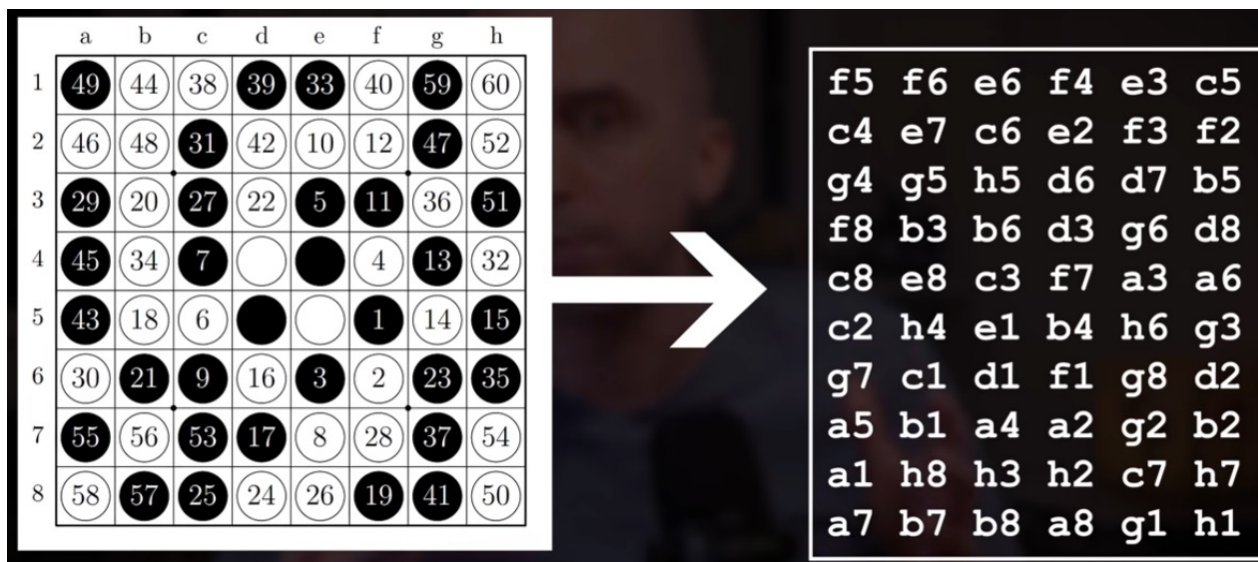
So what does gpt 3.5-turbo-instruct know about chess?

So what does gpt 3.5-turbo-instruct know about chess?

Let us take a simpler neural network: OthelloGPT

2. Ok, but which **internal representation**?

— Let us study a simpler game: **Othello**



Same kind of
algebraic **notation**.
But **simpler**.

Kenneth Li et al. (ICLR-2023) “*Emergent World Representations: Exploring a Sequence Model trained on a Synthetic Task*”

- Ok, but which **internal representation**?



Kenneth Li et al. (ICLR-2023) “*Emergent World Representations: Exploring a Sequence Model trained on a Synthetic Task*”

As a first step, **we train a language model** (a GPT variant we call **Othello-GPT**) to extend partial game transcripts (a list of moves made by players) with legal moves. **The model has no a priori knowledge of the game or its rules.** All it sees during training is a series of tokens derived from the game transcripts. Each token represents a tile where players place their discs. Note that **we do not explicitly train the model to make strategically good moves or to win the game.** Nonetheless, **our model is able to generate legal Othello moves with high accuracy.**

- Ok, but which **internal representation**?

f5	f6	e6	f4	e3	c5
c4	e7	c6	e2	f3	f2
g4	g5	h5	d6	d7	b5
f8	b3	b6	d3	g6	d8
c8	e8	c3	f7	a3	a6
c2	h4	e1	b4	h6	g3
g7	c1	d1	f1	?	
prédisez la suite					

“Our next step is to look for **world representations** that might be used by the network. In Othello, the “world” consists of the current board position. “

- Ok, but which **internal representation**?

f5	f6	e6	f4	e3	c5
c4	e7	c6	e2	f3	f2
g4	g5	h5	d6	d7	b5
f8	b3	b6	d3	g6	d8
c8	e8	c3	f7	a3	a6
c2	h4	e1	b4	h6	g3
g7	c1	d1	f1	?	

prédis la suite

“Our next step is to look for world representations that might be used by the network. In Othello, the “world” consists of the current board position.”

Rk: This is an inexact description.

As we have seen, GPT like models consider first and foremost sequences. But let's go on.

- Ok, but which **internal representation**?

f5	f6	e6	f4	e3	c5
c4	e7	c6	e2	f3	f2
g4	g5	h5	d6	d7	b5
f8	b3	b6	d3	g6	d8
c8	e8	c3	f7	a3	a6
c2	h4	e1	b4	h6	g3
g7	c1	d1	f1	?	

prédisez la suite

“Our next step is to look for world representations that might be used by the network. In Othello, the “world” consists of the current board position.”

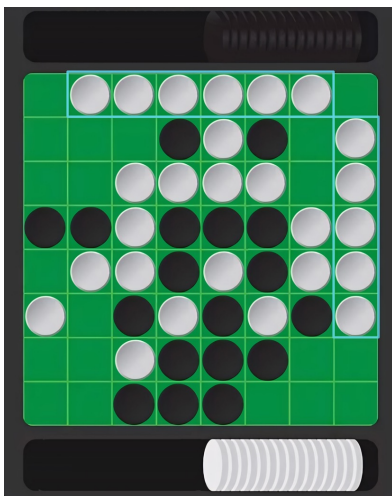
Rk: This is an inexact description.

As we have seen, GPT like models consider first and foremost sequences. But let's go on.

“A natural question is whether, within the model, we can identify a representation of the board state involved in producing its next move predictions.”

- Ok, but which **internal representation**?

How can we do that?



“A natural question is whether, within the model, we can **identify a representation of the board state** involved in producing its next move predictions.”

- Ok, but which **internal representation**?
- Othello-GPT
 - 8-layer GPT model
 - 8-head attention mechanism
 - 512-dimensional hidden space
 - An trainable word embedding of 60 vectors (one for each free tile)
- Training **data**
 - 140,000 games played by **humans**
 - + 20,000,000 **synthetic** games, uniformly sampling leaves from the Othello game tree, reflecting **no strategy**!

Kenneth Li et al. (ICLR-2023) *“Emergent World Representations: Exploring a Sequence Model trained on a Synthetic Task”*

“We now evaluate how well the model’s predictions adhere to the **rules of Othello**.

For each game [in the validation set](#), which was not seen during training, and for each step in the game, **we ask Othello-GPT to predict the next legal move** conditioned by the partial game before that move.

We then calculate **the error rate** by checking if the top-1 prediction is legal. The error rate is **0.01%** for Othello-GPT [trained on the synthetic dataset](#) and **5.17%** for Othello-GPT [trained on the championship dataset](#). For comparison, the untrained Othello-GPT has an error rate of **93.29%**.

The main takeaway is that Othello-GPT does far better than chance in predicting legal moves when trained on both datasets.”

- Ok, but which **internal representation**?

Probing the internal representation

- Ok, but which **internal representation**?

Probing the internal representation

- A **probe** is a classifier (or regressor) whose **input** consists of internal activations of the network, and which is trained to **predict** a feature of interest.
- Here, the probes are trained to **predict the board state** from the network's internal activation (here, with 8 layers) function **after a given sequence of moves**.
- **60 probes** (4 cells are occupied at the start of the game)
 - Each one predict the occupation of a cell **of the board: black, white or empty**
 - From the **internal state** of the neural network on the last hidden layer (here a **512-dimensional** space)

- Ok, but which **internal representation**?

Probing the internal representation

- A **probe** is a classifier (or regressor) whose **input** consists of internal activations of the network, and which is trained to **predict** a feature of interest.
- Here, the probes are trained to **predict the board state** from the network's internal activation (here, with 8 layers) function **after a given sequence of moves**.

	x^1	x^2	x^3	x^4	x^5	x^6	x^7	x^8
Randomized	25.5	25.4	25.5	25.8	26.0	26.2	26.2	26.4
Championship	12.8	10.3	9.5	9.4	9.8	10.5	11.4	12.4
Synthetic	11.3	7.5	4.8	3.4	2.4	1.8	1.7	4.6


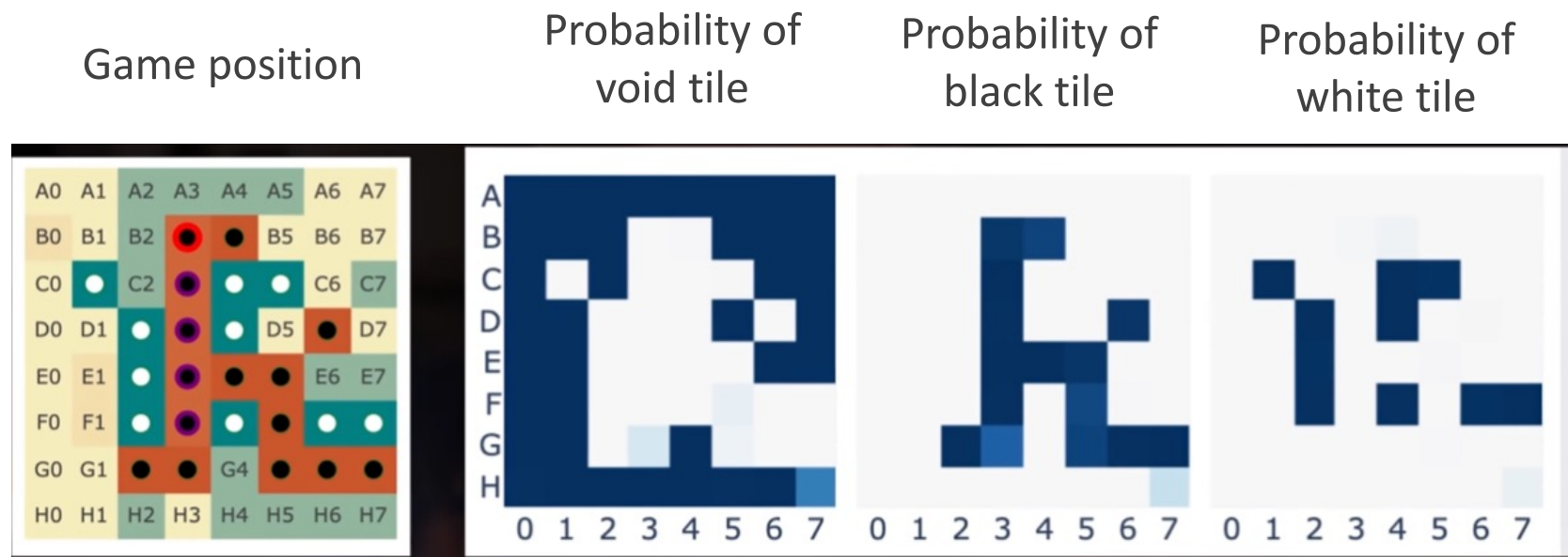


Table 2: Error rates (%) of nonlinear probes on randomized Othello-GPT and Othello-GPTs trained on different datasets across different layers. Standard deviations are reported in Appendix H.

- Ok, but which **internal representation**?

Probing the internal representation

So, it appears that Othello-GPT computes information **reflecting the board state**.



From: Nanda Neel (2023) *“Actually, Othello-GPT has a linear emergent world representation”*

- Clearly **quite remarkable!**
 - The **tokens** are randomly named (e.g. XG103B)
 - At **start**, the probes are random predictors
- The **learned representation** is a mean for the system to be a good predictor
 - This is an **abstract representation** that is **structurally equivalent** to a model of the game

- Ok, but which **internal representation**?

Probing the internal representation

So, it appears that Othello-GPT computes information **reflecting the board state**.

But, how to ensure it?

- Ok, but which **internal representation**?

Probing the internal representation

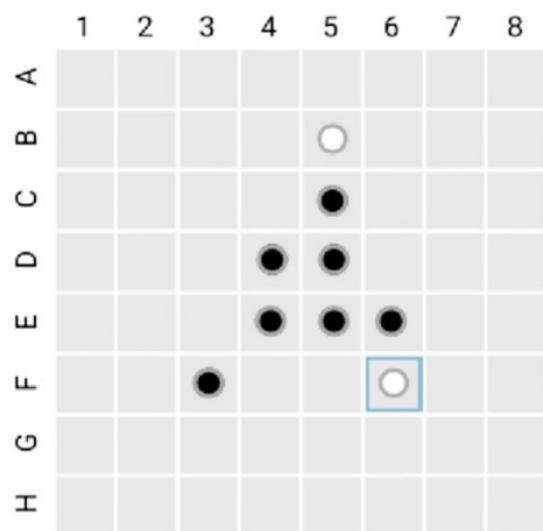
So, it appears that Othello-GPT computes information **reflecting the board state**.

But, how to **ensure** it?

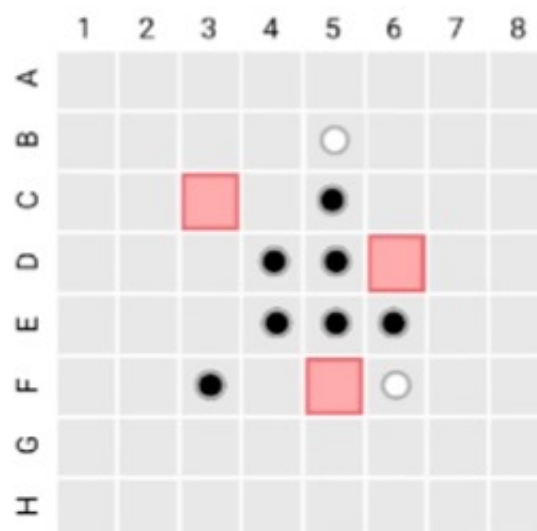
→ Does the internal **representation** have a **causal relationship** with the predicted move?

- Ok, but which **internal representation**?

Does the internal **representation** have a **causal effect**?



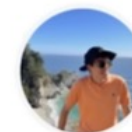
Internal **representation**



Predicted possible moves

Do Large
Language Models
learn world
models or just
surface statistics?

21.JAN.2023 · 15 MIN READ

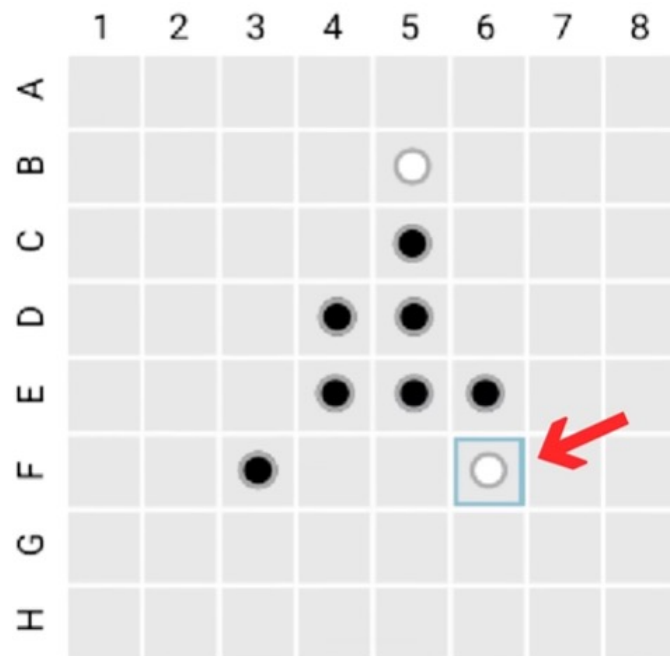


Kenneth Li

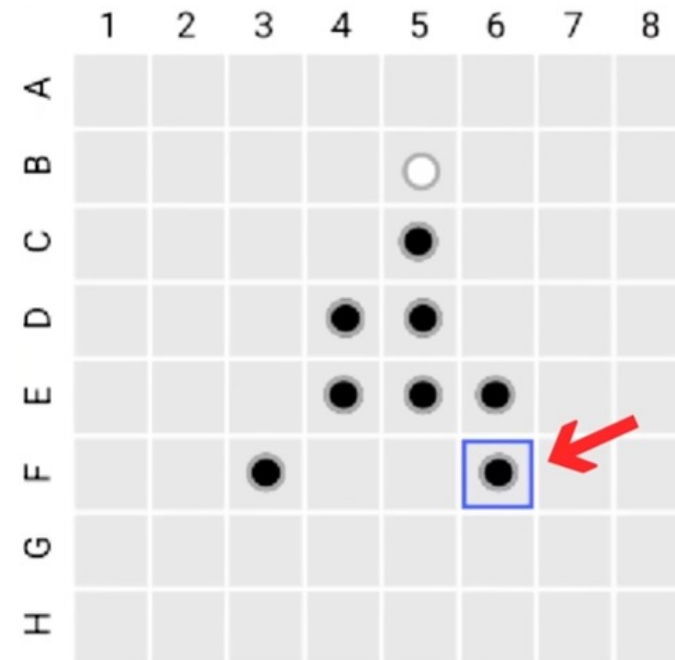
Trying to understand the rich inner world
of deep neural networks.

- Ok, but which **internal representation**?

Does the internal **representation** have a **causal effect**?



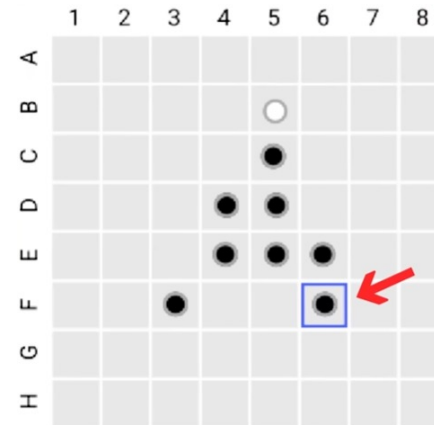
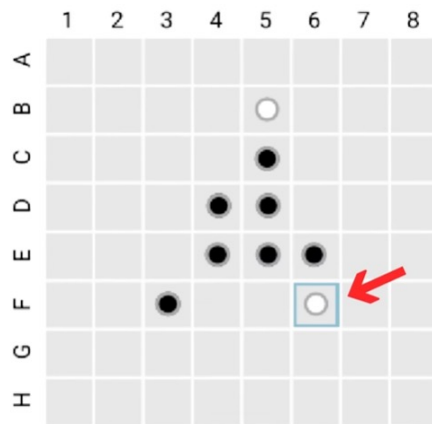
Internal **representation**



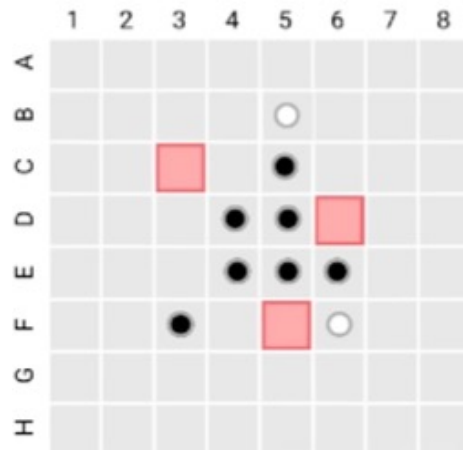
Manually **modified**
representation

- Ok, but which **internal representation**?

Does the internal **representation** have a **causal effect**?



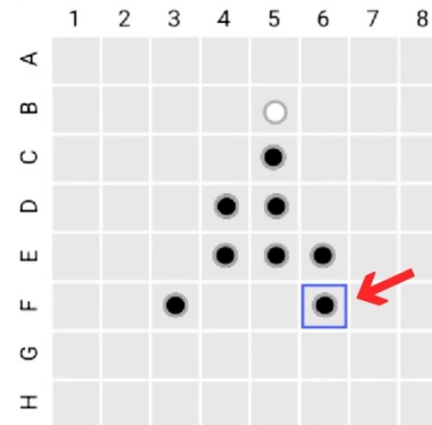
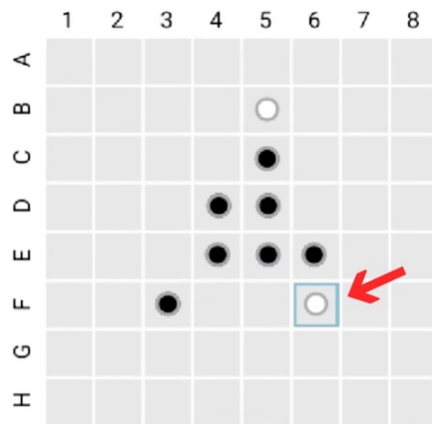
Predicted
possible
moves



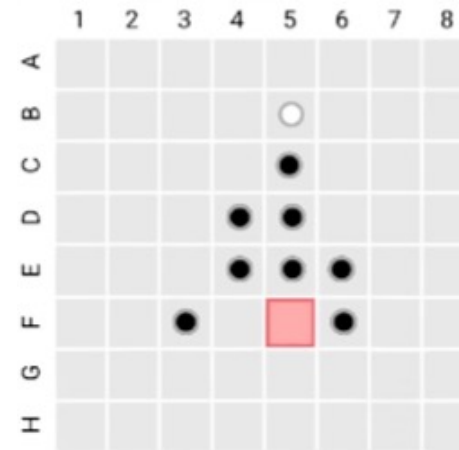
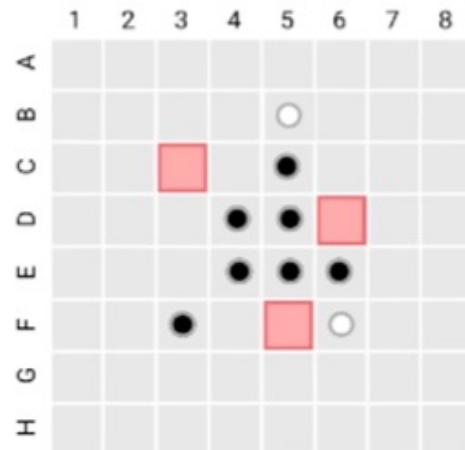
?

- Ok, but which **internal representation**?

Does the internal **representation** have a **causal effect**?



Predicted
possible
moves



- It seems that Othello-GPT has an internal representation of the game

- Ok, but which **internal representation**?

in chess?

- Ok, but which **internal representation**?

in chess?

A **50 million parameter** GPT trained on **5 million games** of chess learns to play at ~1300 Elo in **one day** on **4 RTX 3090 GPUs**.

This model is **only trained to predict the next character in PGN strings** (1.e4 e5 2.Nf3 ...) and is never explicitly given the state of the board or the rules of chess.

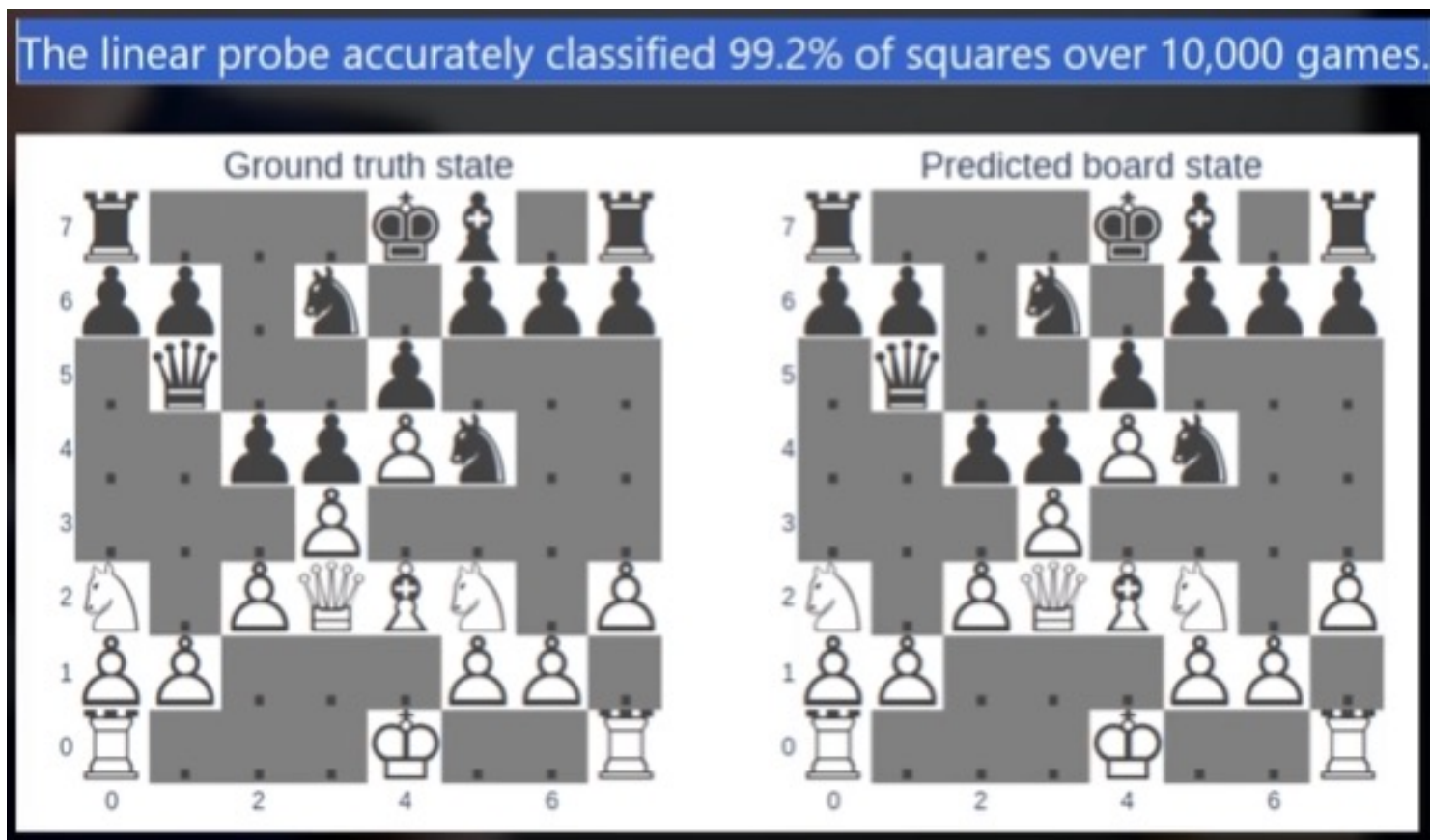
Despite this, in order to better predict the next character, it learns to **compute the state of the board** at any point of the game, and learns a diverse set of rules, including check, checkmate, castling, en passant, promotion, pinned pieces, etc.

In addition, to better predict the next character it **also learns to estimate** latent variables such as **the Elo rating of the players in the game**.



- Ok, but which **internal representation**?

in chess?



- Ok, but which **internal representation**?

in chess?



Original Model
Original Board



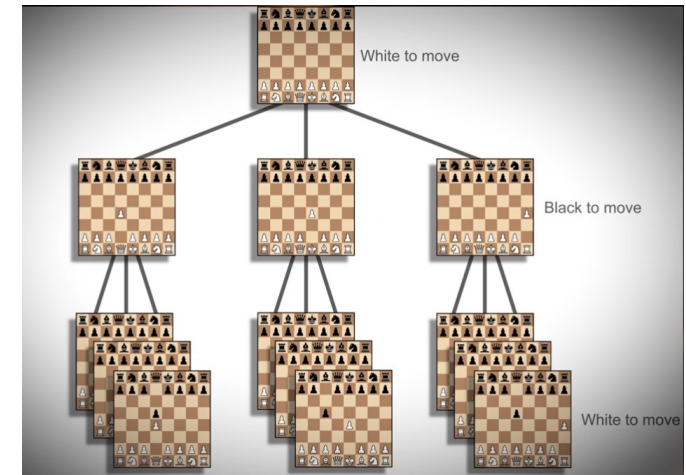
Intervention



Modified Model
Modified Board

LLMs are different from standard AI game players

- They
 - Consider the **sequence** of moves
 - **Not** the actual position
(even though we have seen that ...)



- Do **not** try to **win**.
Only to continue the “game” in the same spirit (choreography?)

Conclusion

- LLMs are like **alien** creatures
 - It is **not straightforward** to conclude whether they know or not to perform some task
 - Inherent **stochasticity**
 - Many **parameters**
 - Requires an empirical approach
 - **Statistical** experiments
 - Exploring the **representations**
 - Looking for **causal** relationships

Conclusion ... No, just a start

- Neel Nanda (<https://www.neelnanda.io/mechanistic-interpretability/othello>)
 - My interpretation of the original paper was that it was strong evidence for the fact that **it's *possible* for "predict the next token" models** to **form world emergent models**, despite never having explicit access to the ground truth of the world/board state.
 - At first glance, playing legal moves in Othello (not even playing *good* moves!) has nothing to do with language models, and I think this is a strong claim worth justifying. **Can working on toy tasks like Othello-GPT really help us to reverse-engineer LLMs like GPT-4?** I'm not sure! But **I think it's a plausible bet** worth making.

Conclusion ... No, just a start

- Neel Nanda (<https://www.neelnanda.io/mechanistic-interpretability/othello>)
 - Within this worldview, **what should our research goals be?**
Fundamentally, I'm an empiricist - models are hard and confusing, it's easy to trick yourself, and often intuitions can mislead. **The core thing of any research project is getting feedback from reality, and using it to form true beliefs about models.** This can either look like forming explicit hypotheses and testing them, or exploring a model and seeing what you stumble upon, but **the fundamental question is whether you have the potential to be surprised and to get feedback from reality.**
 - This means that any project is a trade-off between **tractability** and **relevance** to the end goal.

... and transfer learning?

- Do foundation models learn **universal representation**?
 - ChatGPT 4.0 has an ELO rate of less than 1100
 - Because it is **biased** towards ... chatting
 - The **next frontier** is to be able to adapt ChatGPT online (**continual learning**)
- **Does** learning to play Othello help to learn to play Chess?
- **Does** learning to play Chess help to learn to play Othello?

Bias induced by the **sequence of tasks**

Some **useful facts** about **LLMs** and **Foundation Models**

The **scaling** hypothesis

- By **increasing** (a lot) the **size** of the systems
 - A **phase transition** will appear
 - Corresponding to a **threshold** in the **capacity** of the systems
- Sizes
 - LeNet.5 (1998) : 1,060 parameters
 - AlexNet (2012) : 62,378,344 parameters
 - AlphaGo (2016) : $\sim 65 * 10^6$ parameters
 - GPT1 (2018) : $117 * 10^6$ parameters, trained on 10^9 words
 - GPT2 (2019) : $1.5 * 10^9$ parameters, trained on 6 to $8 * 10^9$ words
 - GPT3 (2020) : $175 * 10^9$ parameters, trained on $250 * 10^9$ words
 - GPT4, Gemini (2023) : $\sim 10^{12}$ parameters, trained on ??? words

The **scaling** hypothesis

- By **increasing** (a lot) the **size** of the systems
 - A **phase transition** will appear
 - Corresponding to a **threshold** in the **capacity** of the systems
- Training time
 - LeNet.5 (1998) : ???
 - AlexNet (2012) : 5 to 6 days on 2 GPUs
 - AlphaGo (2016) : 40 days on 4 TPU (Tensor Processing Units)
 - GPT1 (2018) : 1 day on 1 GPU (10 exaflops)
 - GPT2 (2019) : 1 week on 32 TPuv3 (> 1000 exaflops)
 - GPT3 (2020) : ??? (> 314,000 exaflops)
 - GPT4, Gemini (2023) : ???

- Sources of GPT-3
 - 3% Wikipedia
 - 16% books
 - 22% data base similar to the one used for GPT-2
 - Webpages from Reddit
 - 60% general archives from *Common Crawl*

- **Water consumption**

LI, Pengfei, YANG, Jianyi, ISLAM, Mohammad A., *et al.* Making ai less' thirsty'. *Communications of the ACM*, 2025, vol. 68, no 7, p. 54-61.

- 1 spoon / query
- ~ 1 to 2seconds of a shower / day
- 0.1 one hour of Spotify
- 0.001 one hour of streaming

- **Energy consumption**

- YOU, Josh (2025). *How much energy does ChatGPT use?*. EpochAI, epoch.ai.
- MASLEY, Andy (2025). *Using ChatGPT is not bad for the environment*. The Weird Turn Pro. Andymasley.substack.com
- MASLEY, Andy (2025). *Why Using ChatGPT is not bad for the environment – a cheat sheet*. The Weird Turn Pro. Andymasley.substack.com
- O'DONNELL, James and CROWNHART, Casey (2025). *We did the math on AI's energy footprint. Here's the story you haven't heard*. MIT Technology Review, technologyreview.com

- 0.3 W / query
- 12,000 Wh / day for an average French household
- 98% of the energy consumption comes from the generation of **videos**
 - 15 s. video = 16 km in an electrical vehicle
 - = 3.5 hour of a microwave oven
- Generating **images** costs much less

References

- Acher, Mathieu (2023). [Debunking the Chessboard: Confronting GPTs Against Chess Engines to Estimate ELO Ratings and Assess Legal Move Abilities](#). [Blog.mathieuacher.com](https://blog.mathieuacher.com)
- Burns, C., Izmailov, P., Kirchner, J. H., Baker, B., Gao, L., Aschenbrenner, L., ... & Wu, J. (2023). [Weak-to-strong generalization: Eliciting strong capabilities with weak supervision](#). arXiv preprint arXiv:2312.09390.
- Carlini, Nicholas (2023). [Playing chess with Large Language Models](#). <https://nicholas.carlini.com/writing/2023/chess-llm.html>.
- Karvonen, Adam (2024). [“Chess-GPT’s Internal World Model”](#). https://adamkarvonen.github.io/machine_learning/2024/01/03/chess-world-models.html
- Karvonen, Adam (2024). ["Emergent world models and latent variable estimation in chess-playing language models"](#). arXiv preprint arXiv:2403.15498 (2024).
- Li, Kenneth. ["Do Large Language Models learn world models or just surface statistics?"](#) The Gradient (2023).
- Li, K., Hopkins, A. K., Bau, D., Viégas, F., Pfister, H., & Wattenberg, M. (2022). [Emergent world representations: Exploring a sequence model trained on a synthetic task](#). arXiv preprint arXiv:2210.13382.
- Nanda, Neel. ["Actually, othello-GPT has a linear emergent world representation."](#) Neel Nanda’s Blog 8 (2023).
- RUOSS, Anian, DELÉTANG, Grégoire, MEDAPATI, Sourabh, et al. [Grandmaster-level chess without search](#). CoRR, 2024.